

Quiz 5 - Take-Home - Due by start of class on Wed., Oct. 16, 2019

You may use your textbook and your lecture notes. You may NOT seek help from other people.

Useful Information: $PV = nRT$ $R = 0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}}$ $P_A = \chi_A P_{\text{total}}$ $\chi_A = \frac{n_A}{n_{\text{total}}}$

$E_K = \frac{3}{2} RT$ $v_{\text{rms}} = \sqrt{\frac{3RT}{M}}$ $1 \text{ L} = 1000 \text{ cm}^3 = 0.001 \text{ m}^3$ $1 \text{ atm} = 760 \text{ Torr} = 760 \text{ mm Hg}$

1. Suppose that you perform a chemical reaction that produces toxic hydrogen cyanide (HCN) gas, which you collect in a sealed 1.5-L flask and allow to cool to room temperature.

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- a. If the pressure of HCN in the flask is 215 Torr at 22.5 °C, how many **milligrams** of HCN does the flask contain?

$$V = 1.5 \text{ L} \quad P = 215 \text{ Torr} \left(\frac{1 \text{ atm}}{760 \text{ Torr}} \right) = 0.2829 \text{ atm} \quad T = 22.5^\circ \text{C} = 295.65 \text{ K}$$

$$n = \frac{PV}{RT} = \frac{(0.2829 \text{ atm})(1.5 \text{ L})}{(0.08206 \frac{\text{L} \cdot \text{atm}}{\text{mol} \cdot \text{K}})(295.65 \text{ K})} = 0.01749 \text{ mol}$$

$$\text{Molar mass} = 1.0079 + 12.011 + 14.0067 = 27.0256 \text{ g/mol}$$

$$0.01749 \text{ mol} \left(\frac{27.0256 \text{ g}}{1 \text{ mol HCN}} \right) \left(\frac{1000 \text{ mg}}{1 \text{ g}} \right) = 4.7 \times 10^2 \text{ mg}$$

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- b. Suppose that the flask breaks, releasing all of the HCN into the (enclosed) room. If the room volume is 75 m³, what is the new gas pressure?

$$\frac{P_1 V_1}{n_1 T_1} = \frac{P_2 V_2}{n_2 T_2} \quad n_1 = n_2 \quad T_1 = T_2 \quad \rightarrow \quad P_1 V_1 = P_2 V_2$$

$$P_1 = 0.2829 \text{ atm} \quad V_1 = 1.5 \text{ L}$$

$$V_2 = 75 \text{ m}^3 \left(\frac{1 \text{ L}}{0.001 \text{ m}^3} \right) = 7.5 \times 10^4 \text{ L}$$

$$P_2 = \frac{P_1 V_1}{V_2} = \frac{(0.2829 \text{ atm})(1.5 \text{ L})}{7.5 \times 10^4 \text{ L}} = 5.7 \times 10^{-6} \text{ atm}$$

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- c. Due to the risk of thyroid, blood, and respiratory effects, the National Institute for Occupational Safety and Health (NIOSH) has established a recommended exposure limit for HCN of 5 $\frac{\text{mg}}{\text{m}^3}$.

Would your exposure exceed this limit? (Be sure to show your work.)

$$\frac{473 \text{ mg HCN}}{75 \text{ m}^3 \text{ room vol.}} = 6.3 \frac{\text{mg}}{\text{m}^3}$$

Yes; your exposure would exceed the limit.

Quiz continues on reverse side

2. Suppose that you fill a tire with air to a pressure of 36.7 psi (pounds per square inch; 1 atm = 14.70 psi) when the temperature is 22.1 °C.

a. Nitrogen (N₂), oxygen (O₂) and argon (Ar) are the most prevalent gases in air. If the mole fraction of N₂ in the mixture is 0.79, what is the **partial pressure of N₂** in the tire?

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$$X_{N_2} = 0.79 \quad P_{\text{total}} = 36.7 \text{ psi} \quad P_{N_2} = ?$$

$$P_{N_2} = X_{N_2} P_{\text{total}}$$

$$P_{N_2} = (0.79)(36.7 \text{ psi}) = 29 \text{ psi} \quad (\text{or } 2.0 \text{ atm})$$

b. How do the **average kinetic energies** of the nitrogen and oxygen molecules compare? **Explain** in a few words.

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They are the same. $\overline{E_k}$ depends only on temp.

($\overline{E_k} = \frac{3}{2} RT$), which is the same for both gases.

c. Which of the three gases in the mixture has particles moving at the **fastest average speed**, nitrogen, oxygen, or argon? **Explain** briefly.

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$$v_{\text{rms}} = \sqrt{\frac{3RT}{M}}$$

The gas with the smallest molar mass will have the fastest average speed, v_{rms} .

$$M_{N_2} \sim 28 \text{ g/mol}$$

$$M_{O_2} \sim 32 \text{ g/mol}$$

$$M_{Ar} \sim 40 \text{ g/mol}$$

Here, N₂ is the lightest and fastest.

(Lots of extra space here!)