

KEY**Question 1: (10 points)**

Circle those units below (and only those units) which have dimensionality of energy. They need not be units that are commonly used or which we mentioned in class:

$\text{kW} \cdot \text{hr}$ / hp J N
GJ lb Btu Quad
calorie / N/m J ft · lb/s
W nN MW MTOE

Question 2 (10 points)

The most significant aspect of world consumption of energy over the last 40 years has been the b.

- a. growth of nuclear power
- ☒ b. expanding use of oil
- c. increased use of coal
- d. emphasis on energy conservation
- e. increase in our fossil fuel reserves

Problem 1 (20 points)

The power to a 1500W space heater in a dorm room is left on for three months during the winter.

a) Calculate the electrical energy consumed by the heater, in both kW•hr and Btu.

$$\begin{aligned}
 P &= E/t \rightarrow E = Pt \\
 &= 1500\text{W} \times 3\text{months} \times \left(\frac{\text{kW}}{1000\text{W}}\right) \times \left(\frac{30\text{days}}{\text{month}}\right) \times \left(\frac{24\text{h}}{\text{day}}\right) \\
 P &= 3240\text{kWh} \\
 3240\text{kWh} \times \left(\frac{3413\text{Btu}}{\text{kWh}}\right) &= 1.11 \times 10^7\text{Btu}
 \end{aligned}$$

b) In NY state, residential customers pay nearly \$0.18/kW•hr. Calculate the power bill (in dollars) for this space heater for three months. (Notice that the money wasted by the heater is about 2/3 of this value, if we assume electricity to be about 3' as expensive as whatever primary fuel is used in heating the dorms.)

$$\text{Cost} = \frac{0.18}{\text{kWh}} \cdot 3240\text{kWh} = \$583.$$

Problem 2 (20 points)

World energy use is about 500Quad/yr. Translate that into Watts.

$$P = \frac{E}{t} = \frac{500 \text{ Quad}}{1 \text{ year}} \times \frac{10^{15} \text{ Btu}}{\text{quad}} \times \frac{1055 \text{ J}}{\text{Btu}} \times \frac{1 \text{ yr}}{365 \text{ day}} \times \frac{\text{day}}{24 \text{ h}} \times \frac{\text{hr}}{60 \text{ min}} \times \frac{\text{min}}{\text{sec}}$$

$$P = 1.7 \times 10^{13} \text{ W} = 17 \text{ Terawatt.}$$

Problem 3 (20 points)

The position of a particular particle as a function of time is given by

$$\vec{r} = (9.60t \hat{i} + 8.85\hat{j} - 1.00t^2 \hat{k}) \text{ m.}$$

a) Determine the particle's velocity as a function of time and

$$\vec{v} = \frac{d\vec{r}}{dt} = (9.60 \hat{i} - 2.00t \hat{k}) \text{ m/s}$$

b) acceleration as a function of time.

$$\vec{a} = \frac{d\vec{v}}{dt} = (-2.00 \hat{k}) \text{ m/s}^2$$

Problem 4 (20 points)

A 380-kg piano slides 3.9 m down a 27° incline and is kept from accelerating by a man who is pushing back on it parallel to the incline. Ignore friction.

Determine:

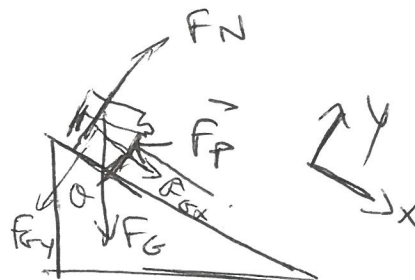
(a) the force exerted by the man,

$$\sum F = ma$$

$$x : F_{gx} - F_p = ma = 0$$

$$mg \sin \theta = F_p$$

$$F_p = (380 \text{ kg})(9.8 \text{ m/s}^2) \sin 27^\circ = 1690.6 \text{ N}$$



(b) the work done by the man on the piano,

$$W_p = F_p d \cos 180^\circ = -(1690.6 \text{ N})(3.9 \text{ m}) = -6593.5 \text{ J}$$

(c) the work done by the force of gravity,

$$W_{F_g} = F_g d \cos \theta ; \theta = 90^\circ - 27^\circ = 63^\circ$$

$$W_{F_g} = mg d \cos \theta = (380 \text{ kg})(9.8 \frac{\text{m}}{\text{s}^2})(3.9) \cos 63^\circ = 6593.5 \text{ J}$$

and (d) the net work done on the piano.

$$W_{\text{piano}} = W_{\text{net}} = \cancel{W_{F_N}} + W_{F_p} + \cancel{W_{F_{gy}}} + W_{F_{gx}}$$

$$W_{\text{piano}} = -6593.5 \text{ J} + 6593.5 \text{ J} = 0 \text{ J} \quad (\text{No work done on the piano})$$

Equations

$$\begin{aligned}
 v_x &= v_{0x} + a_x t & x &= x_0 + v_{0x} t + \frac{1}{2} a_x t^2 & v_{avg} &= \frac{\Delta r}{\Delta t}, v_{ins} = \frac{dr}{dt} \\
 v_y &= v_{0y} + a_y t & y &= y_0 + v_{0y} t + \frac{1}{2} a_y t^2 & a_{avg} &= \frac{\Delta v}{\Delta t}, a_{ins} = \frac{dv}{dt} & v_x^2 &= v_{0x}^2 + 2a_x(x - x_0) \\
 & & & & & & v_y^2 &= v_{0y}^2 + 2a_y(y - y_0) \\
 & & & & & & \Delta \vec{r} &= \vec{r}_f - \vec{r}_i
 \end{aligned}$$

$$\begin{aligned}
 \sum \vec{F} &= m\vec{a} \\
 \sum F_x &= ma_x & g &= 9.8 \text{ m/s}^2 \\
 \sum F_y &= ma_y & W &= F_g = mg
 \end{aligned}$$

Potential energy:Gravitational Potential energy: $U = mgy$

Conservation of Energy:

For conservative forces: $K_2 + U_2 = K_1 + U_1$ Translational Kinetic Energy: $K = \frac{1}{2} mv^2$ Work: $W = Fd \cos\theta = \vec{F} \cdot \vec{d}$ Power: $P = \frac{dW}{dt} = Fv$